

# Polynomial expression

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## Polynomial expression

A polynomial expression  $S(x)$  in one variable  $x$  is an algebraic expression in  $x$  term as

$$S(x) = a_n x^n + a_{n-1} x^{n-1} + a_{n-2} x^{n-2} + \dots + ax + a_0$$

Where  $a_n, a_{n-1}, \dots, a_1, a_0$  are constant and real numbers and  $a_n$  is not equal to zero

Some important points to remember

- 1)  $a_n, a_{n-1}, a_{n-2}, \dots, a_1, a_0$  are called the coefficients for  $x^n, x^{n-1}, \dots, x^1, x^0$
- 2)  $n$  is called the degree of the polynomial
- 3) when  $a_n, a_{n-1}, a_{n-2}, \dots, a_1, a_0$  all are zero, it is called zero polynomial
- 4) A constant polynomial is the polynomial with zero degree, it is a constant value polynomial
- 5) A polynomial of one item is called monomial, two items binomial and three items as trinomial
- 6) A polynomial of one degree is called linear polynomial, two degree as quadratic polynomial and degree three as cubic polynomial

## Zero's or roots of the polynomial

It is a solution to the polynomial equation  $S(x)=0$  i.e. a number "a" is said to be a zero of a polynomial if  $S(a) = 0$ .

If we draw the graph of  $S(x) = 0$ , the values where the curve cuts the X-axis are called Zeros of the polynomial

- a) Linear polynomial has only one root
- b) A zero polynomial has all the real number as roots
- c) A constant polynomial has no zeros

## Remainder Theorem's

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If  $p(x)$  is a polynomial of degree greater than or equal to 1 and  $p(x)$  is divided by the expression  $(x-a)$ , then the remainder will be  $p(a)$

Factor's Theorem's

If  $x-a$  is a factor of polynomial  $p(x)$  then  $p(a)=0$  or if  $p(a) =0$ ,  $x-a$  is the factor the polynomial  $p(x)$

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