

# Similar triangles Questions

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## Question 1.

In  $\Delta ABC$ , ray  $AD$  bisects  $\angle A$  and intersects  $BC$  in  $D$ . If  $BC = a$ ,  $AC = b$  and  $AB = c$ , prove that:

$$(i) \quad BD = \frac{ac}{b+c}$$

$$(ii) \quad DC = \frac{ab}{b+c}$$

## Question 2.

Two poles of heights  $a$  and  $b$  metres are standing vertically on a level ground  $r$  metres apart. Prove that the height  $c$  of the point of intersection of the lines joining the top of each pole to the foot of the opposite pole is given by  $\frac{ab}{a+b}$ , i. e.,  $c = \frac{ab}{a+b}$ .

## Question 3.

$D$  and  $E$  are points on the sides  $CA$  and  $CB$  respectively of  $\Delta ABC$  right – angled at  $C$ . Prove that  $AE^2 + BD^2 = AB^2 + DE^2$

## Question 4.

In a quadrilateral  $\Delta ABCD$ ,  $\angle B = 90^\circ$ ,  $AD^2 = AB^2 + BC^2 + CD^2$ , prove that  $\angle ACD = 90^\circ$

## Question 5.

$ABC$  is a triangle in which  $AB = AC$  and  $D$  is a point on  $AC$  such that  $BC^2 = AC \times CD$ . Prove that  $BD = BC$

## Question 6.

$P$  and  $Q$  are the mid points on the sides  $CA$  and  $CB$  respectively of triangle  $ABC$  right angled at  $C$ . Prove that

$$4(AQ^2 + BP^2) = 5 AB^2$$

## Question 7.

### True and False statement

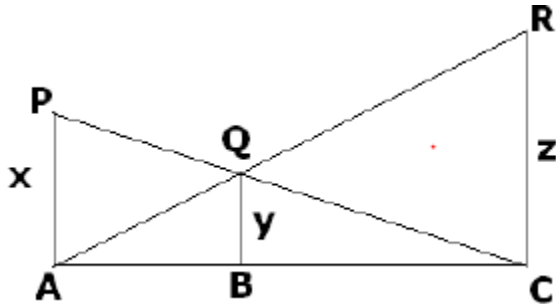
- a) All quadrilateral triangles are similar.
- (b) All circles are similar.
- (c) All isosceles triangles are similar.

(d) All  $30^\circ$ .  $60^\circ$ .  $90^\circ$  triangles are similar.

**Question 8.**

In the below figure PA, QB and RC are each perpendicular to AC.

Prove that  $1/x + 1/y = 1/z$



**Question 9.**

ABC is a right triangle right angled at C. Let  $BC = a$ ,  $CA = b$   $AB = c$  and let  $p$  be the length of perpendicular from C on AB, prove that

(i)  $cp = ab$

(ii)  $1/p^2 = 1/a^2 + 1/b^2$

**Question 10.**

Diagonals of a trapezium ABCD with  $AB \parallel DC$  intersect each other at the point O. If  $AB = 2DC$ , find ratio of the areas of AOB and COD