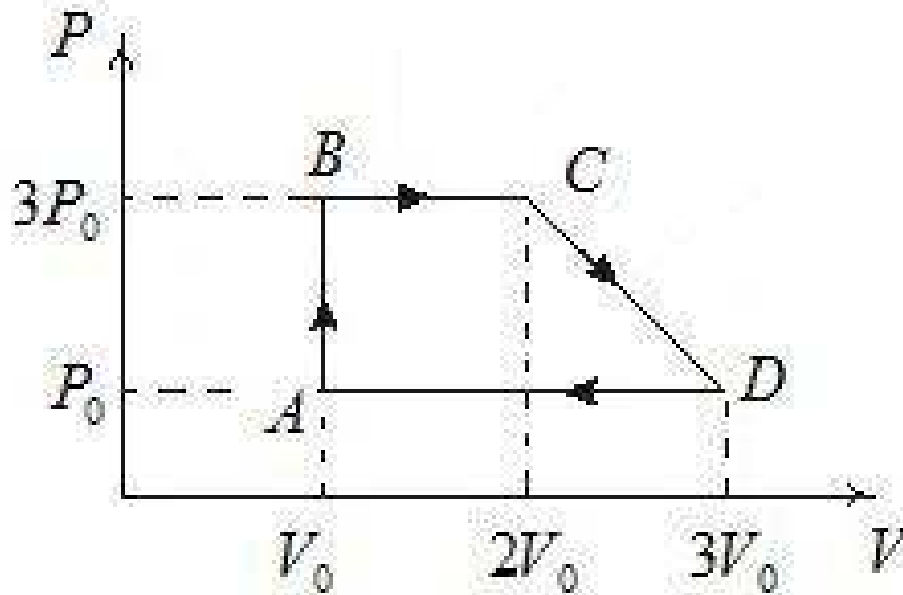


Thermodynamics Problem's

Question: One mole of an ideal monoatomic gas is taken round the cyclic process ABCDA as shown in figure.

- A) Work done by the gas
- b Heat absorbed by the gas in AB and BC
- c. Heat in process CD
- d. Find the temperature at C and D
- e. Maximum temperature attained by the gas during the cycle
- f. Net change in the internal energy and the heat



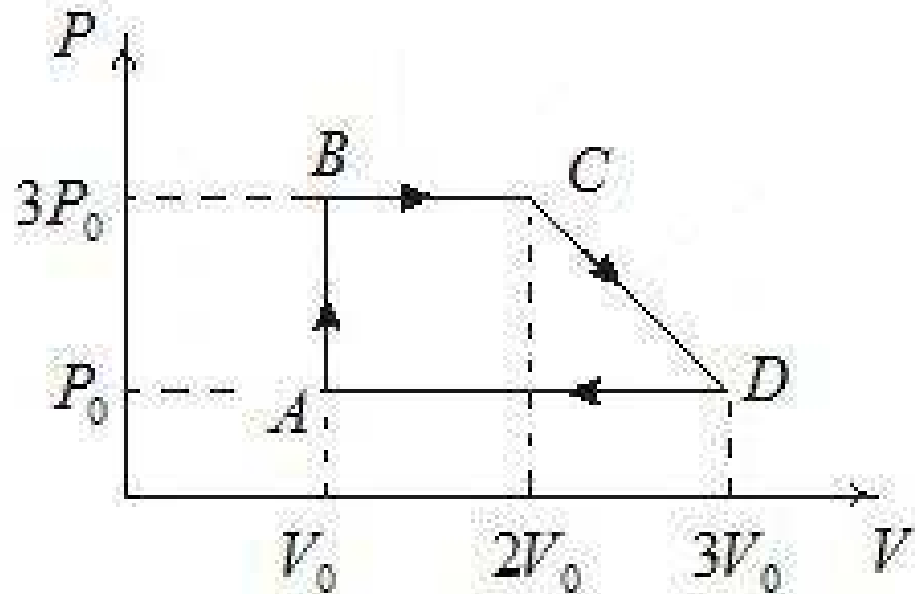
Solution

For monoatomic gas

$$C_p = 5R/2$$

$$C_v = 3R/2$$

a) Work done by the gas = Area enclosed by the curve ABCDA
 $= 3P_0V_0$



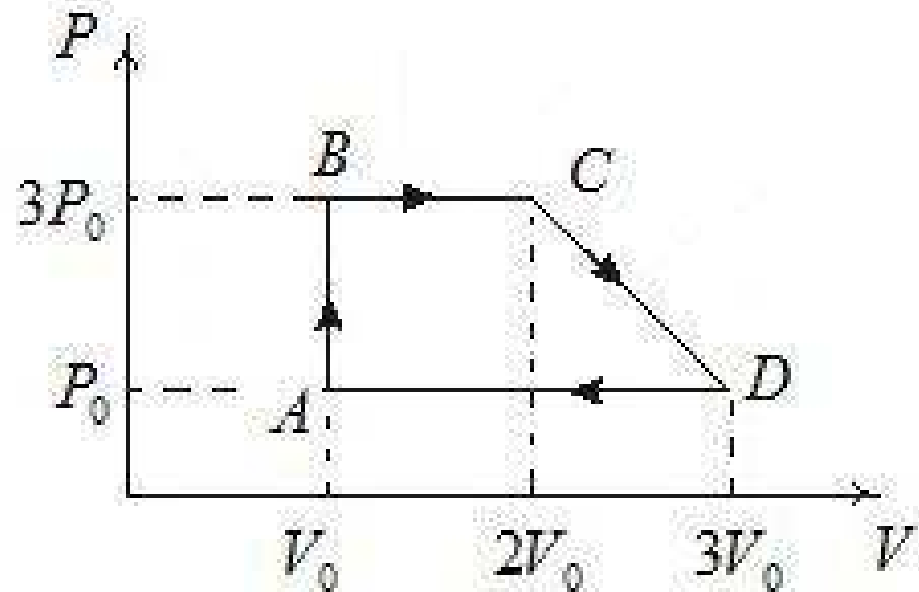
Solution continued

- Heat absorbed the gas in AB

$$\begin{aligned} Q_{AB} &= C_V(T_B - T_A) \\ &= (3R/2)(3P_0V_0/R - P_0V_0/R) \\ &= 3P_0V_0 \end{aligned}$$

Heat absorbed the gas in BC

$$\begin{aligned} Q_{BC} &= C_P(T_C - T_B) \\ &= (5R/2)(6P_0V_0/R - 3P_0V_0/R) \\ &= 15P_0V_0/2 \end{aligned}$$



Solution continued

- Heat rejected in DA

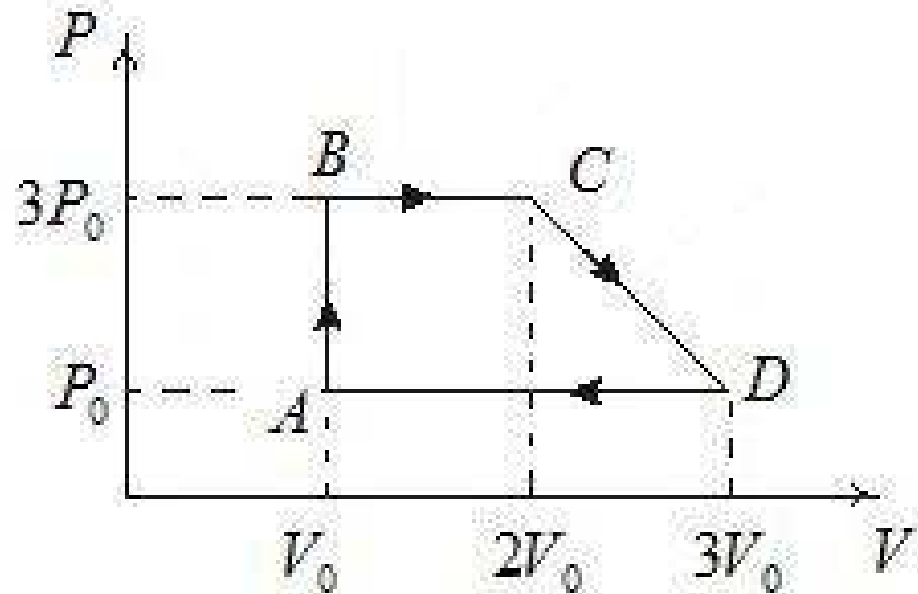
$$Q_{DA} = C_P (T_A - T_D) \\ = -5P_0V_0$$

Now for the cycle process

$$Q_{AB} + Q_{BC} + Q_{CD} + Q_{DA} = W$$

So

$$Q_{CD} = -5P_0V_0/2$$

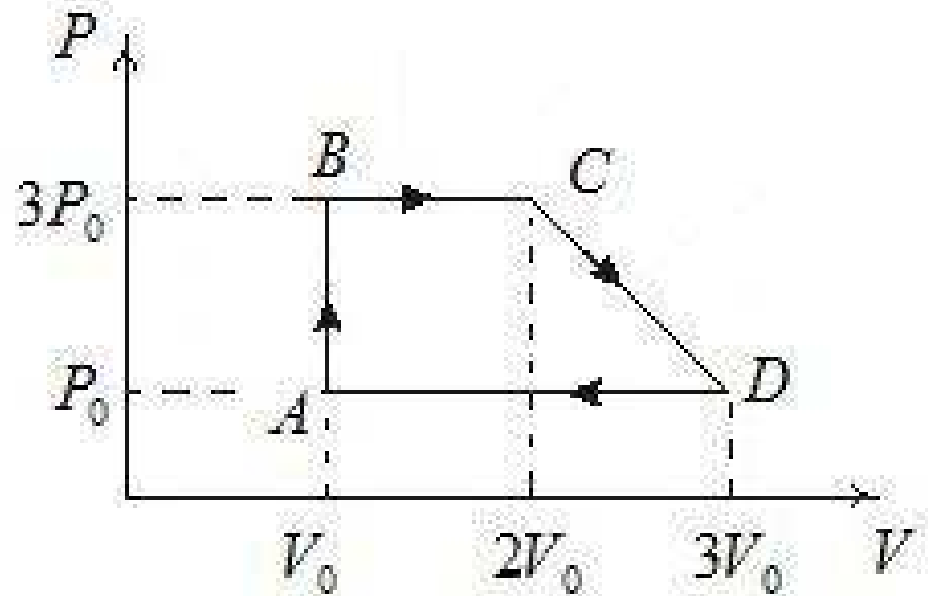


Solution continued

- from diagram and $PV=RT$

$$T_C = 6P_0V_0/R$$

$$T_D = 3P_0V_0/R$$



Solution Continued

- Max temperature will be on the slope CD

Equation of Slope CD as Coordinated system

$$y = mx + c$$

- Taking the values for C and D, we get

$$P = -(2P_0/V_0)V + 7P_0$$

Now $PV = RT$

So

$$RT = -(2P_0/V_0)V^2 + 7P_0V$$

For max

dT/dV should be zero

$$\text{So } R \frac{dT}{dV} = -4P_0 \frac{V}{V_0} + 7P_0$$

$$V = 7V_0/4$$

$$T_{\text{max}} = 49P_0V_0/4R$$

f. $\Delta U = 0$

Net heat = $3P_0V_0$

