

Quadratic Equation

Quadratic Polynomial

$$P(x) = ax^2 + bx + c \quad \text{where } a \neq 0$$

Quadratic equation

$$ax^2 + bx + c = 0 \quad \text{where } a \neq 0$$

Solution or root of the Quadratic equation

A real number α is called the root or solution of the quadratic equation if

$$a\alpha^2 + b\alpha + c = 0$$

Some other points to remember

- The root of the quadratic equation is the zeroes of the polynomial $p(x)$.
- We know from chapter two that a polynomial of degree n can have maximum n zeroes. So a quadratic equation can have maximum two roots
- A quadratic equation has no real roots if $b^2 - 4ac < 0$

How to Solve Quadratic equation

S.no	Method	Working
1	factorization	This method we factorize the equation by splitting the middle term b

		<p>In $ax^2+bx+c=0$</p> <p>Example</p> $6x^2-x-2=0$ <p>1) First we need to multiple the coefficient a and c. In this case $=6 \times -2 = -12$</p> <p>2) Splitting the middle term so that multiplication is 12 and difference is the coefficient b</p> $6x^2 + 3x - 4x - 2 = 0$ $3x(2x+1) - 2(2x+1) = 0$ $(3x-2)(2x+1) = 0$ <p>3) Roots of the equation can be find equating the factors to zero</p> $3x-2=0 \Rightarrow x=2/3$ $2x+1=0 \Rightarrow x=-1/2$
2	Square method	<p>In this method we create square on LHS and RHS and then find the value.</p> $ax^2 + bx + c = 0$ <p>1) $x^2 + (b/a)x + (c/a) = 0$</p> <p>2) $(x + b/2a)^2 - (b/2a)^2 + (c/a) = 0$</p> <p>3) $(x + b/2a)^2 = (b^2 - 4ac) / 4a^2$</p> <p>4) $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$</p> <p>Example</p> $x^2 + 4x - 5 = 0$

		<p>1) $(x+2)^2 - 4 - 5 = 0$</p> <p>2) $(x+2)^2 = 9$</p> <p>3) Roots of the equation can be find using square root on both the sides</p> <p>$x+2 = -3 \Rightarrow x = -5$</p> <p>$x+2 = 3 \Rightarrow x = 1$</p>
3	Quadratic method	<p>For quadratic equation</p> <p>$ax^2 + bx + c = 0$,</p> <p>roots are given by</p> $x = \frac{-b + \sqrt{b^2 - 4ac}}{2a}, x = \frac{-b - \sqrt{b^2 - 4ac}}{2a}$ <p>For $b^2 - 4ac > 0$, Quadratic equation has two real roots of different value</p> <p>For $b^2 - 4ac = 0$, quadratic equation has one real root</p> <p>For $b^2 - 4ac < 0$, no real roots for quadratic equation</p>

Nature of roots of Quadratic equation

S.no	Condition	Nature of roots
1	$b^2 - 4ac > 0$	Two distinct real roots
2	$b^2 - 4ac = 0$	One real root
3	$b^2 - 4ac < 0$	No real roots